

Inferential Expressivism and the Negation Problem

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Abstract

We develop a novel solution to the negation version of the Frege–Geach problem by taking up recent insights from the bilateral programme in logic. Bilateralists derive the meaning of negation from a primitive *B-type* inconsistency involving the attitudes of assent and dissent. Some may demand an explanation of this inconsistency in simpler terms, but we argue that bilateralism’s assumptions are no less explanatory than those of *A-type* semantics that only require a single primitive attitude, but must stipulate inconsistency elsewhere. Based on these insights, we develop a version of B-type expressivism called *inferential expressivism*. This is a novel semantic framework that characterises meanings by inferential roles that define which *attitudes* one can *infer* from the use of terms. We apply this framework to normative vocabulary, thereby solving the Frege–Geach problem generally and comprehensively. Our account moreover includes a semantics for epistemic modals, thereby also explaining normative terms under epistemic modals.

1 Introduction

Expressivism about a class of linguistic terms holds that the meaning of these terms is to be explained by appealing to the mental *attitudes* that these terms are used to express. Historically, expressivism has been applied to normative terms by taking, say, *wrong* to express the non-cognitive (desire-like) attitude of *disapproval*¹ (Hare, 1952), but has more recently been exten-

¹We stipulatively call the attitude expressed by *wrong* ‘disapproval’, but any other term would do.

ded to other terms (e.g. Humberstone, 2000; Schnieder, 2010; Yalcin, 2012). Expressivism is appealing and entrenched, but—no matter its application—must contend with the *Frege–Geach embedding problem* (Frege, 1919; Geach, 1965; Schroeder, 2008b). The goal of this paper is to use insights from expressivism about negation to develop a novel form of expressivism about normative terms. As we shall show, this novel form of expressivism has the resources to solve the Frege–Geach problem generally and comprehensively.

In its original version, the Frege–Geach problem challenges the expressivist to explain how a term that putatively expresses an attitude can embed in conditional antecedents. However, current debate centres on the *negation version* of the Frege–Geach problem (Unwin, 1999, 2001; Schroeder, 2008a). In brief, it goes as follows. As we rehearse in Section 2, the negation of a descriptive term appears to be different from the negation of a term that (putatively) is treated in expressivist terms. To wit, the two normative claims *Murdering is wrong* and *Murdering is not wrong*, if receiving expressivist treatment, must be read as expressing *different attitudes* towards the *same content*. Thus, it seems that *not* here modifies attitudes. However, in the descriptive claims *Murdering is legal* and *Murdering is not legal*, the term *not* modifies the *content* of what is claimed. The expressivist is challenged to explain these facts without any *ad hoc* stipulations. The problem permeates semantic analysis on different levels; we discuss its different aspects in Section 2.

We propose to solve the negation problem by adopting the framework of *inferential expressivism*. Inferential expressivism is a general semantic framework that grows out of the bilateral programme in logic (Rumfitt, 2000; Incurvati and Schlöder, 2017). Very briefly, expressivism explains terms by reference to the attitudes they are used to express, inferentialism explains terms by reference to the inferences they feature in, and inferential expressivism explains terms by reference to what attitudes one can infer from their use. The possibility of combining expressivism with inferentialism is acknowledged (Chrisman, 2008; Baker and Woods, 2015; Tiefensee, 2016), but we are the first to develop it systematically and to give all formal details of an inferential expressivist account of normative language. Moreover, our inferential expressivism includes an account of epistemic modals (Incurvati and Schlöder, Forthcoming). Building on this prior work, our account also explains how epistemic modals interact with

normative vocabulary, improving on the analysis of Mark Schroeder (2008a), which encounters difficulties with sentences like *Murdering might be wrong*.

Our inferential expressivism allows us to locate the difference between normative and descriptive vocabulary *entirely* at the level of lexical semantics. To wit, on our account uttering a declarative sentence standardly expresses *assent* to a proposition, where the meaning of that proposition is given by inference rules. Descriptive terms have *attitude invariant* inferential semantics; e.g., the semantics of *bachelor* is such that from the expression of assent to $\lceil \textit{John is a bachelor} \rceil$ one can infer assent to $\lceil \textit{John is unmarried} \rceil$.² In contrast, normative terms have *attitude changing* inferential semantics; the term *wrong* receives an inferential semantics such that from assent to $\lceil \textit{murdering is wrong} \rceil$ one infers the different attitude *disapproval* towards $\lceil \textit{murdering} \rceil$. This is the only difference needed to define inferential expressivist semantics for logical operators—in particular, negation—that behave as they should.

In the next section we describe the different aspects of the negation problem in detail. Then, in Section 3, we introduce inferential expressivism, extend it to a semantics for normative vocabulary like *wrong*, and discuss how this solves the negation problem. Finally, we compare our approach to Schroeder's (2008a) influential solution in Section 4, arguing that we improve on his account by solving what he calls the *new new negation problem* related to normative sentences involving epistemic modals. We conclude in Section 5 by locating inferential expressivism within the metaethical landscape.

2 The negation problem

Expressivists claim that a sentence like *Murdering is wrong* (1a) is used to express the attitude of *disapproval* towards the act of murdering. The expressivist problem with negation is to explain what is expressed by *Murdering is not wrong* (1b). There is one clear constraint on any such explanation: to utter both (1a) and (1b) sounds *inconsistent* and this fact ought to be

²In order to distinguish sentences from what they express, we encase contents one can have attitudes (both cognitive and non-cognitive) towards in Gödel brackets; e.g. asserting *John is unmarried* expresses assent to the proposition $\lceil \textit{John is unmarried} \rceil$. Formulae and variables generally stand for such contents, so we do not bracket them.

explained.³

- (1) a. Murdering is wrong.
- b. Murdering is not wrong.
- c. Not murdering is wrong.
- d. Not murdering is not wrong.

Which attitude is expressed by (1b)? It cannot be *disapproval of not murdering*, since that is what one expresses by uttering (1c). It is a mistake to equate (1b) with (1c), since (1c) is inconsistent with (1d), whereas (1b) is not. Moreover, (1b) cannot express the *absence of disapproval of murdering*, as this would wrongly conflate (2a) and (2b).

- (2) a. Jane does not think that murdering is wrong. = Jane does not disapprove of murdering
- b. Jane thinks that murdering is not wrong. = ?
- c. Jane thinks that murdering is wrong. = Jane disapproves of murdering
- d. Jane thinks that not murdering is wrong. = Jane disapproves of not murdering

Nick Unwin (1999, 2001) notes that the problem is really quite simple: in *Jane does (not) think that (not) murdering is (not) wrong* one can insert up to three negations, and no two choices should be equivocated. But the expressivist paraphrase *Jane does (not) disapprove of (not) murdering* only has space for two, so the expressivist requires an attitude other than disapproval to describe what attitude is expressed by (1b). One may—by stipulation—call this attitude *tolerance* and describe (1b) as the expression of tolerance towards the act of murder. However, according to Schroeder (2008a), this leaves an explanatory gap. We observed that *Murdering is wrong* and *Murdering is not wrong* are inconsistent—the expressivist needs to explain this fact. She may attempt to do so by claiming that it is inconsistent to simultaneously tolerate and disapprove of the same act, in much the same way that it is inconsistent to hold the attitude of belief towards two inconsistent contents or the attitude of intent towards two incompatible goals.

³Here, ‘inconsistent’ is used pre-theoretically. We discuss the different relevant notions of inconsistency in due course.

Schroeder (2008a), however, argues that this does not suffice. Any putative such explanation appears to entail that the expressivist is committed to there being two ways for attitude expressions to be inconsistent. First, *A-type* inconsistency, which arises from holding a single kind of *inconsistency-transmitting* attitude, such as belief, towards truth-conditionally inconsistent contents (e.g. it is A-type inconsistent to believe both *p* and *not p*). Second, *B-type* inconsistency, which arises from holding different kinds of attitude that are in some sense mutually exclusive towards the *same* content. The supposed explanation of the inconsistency of (1a) and (1b)—that they express, respectively, disapproval and tolerance of the same act—is B-type. A-type inconsistencies arise in descriptive language: the propositional contents of (3a) and (3b) are inconsistent and hence it is inconsistent to express belief in both.

(3) a. Murdering is legal.

b. Murdering is not legal.

A-type inconsistency feels familiar, whereas B-type inconsistency may appear to be an artifact of expressivism. The expressivist cannot, Schroeder (2008a) contends, create the attitude of tolerance and its B-type properties by *fiat*. Rather, she needs to explain *why* there is an attitude that behaves like what she calls *tolerance*—by appealing to more fundamental concepts. To find these concepts or to explain away the complaint is the *negation problem*.

The expressivist, however, may point to natural cases of B-type inconsistencies. For example, *believing p* and *wondering whether p* seem to be B-type inconsistent attitudes, regardless of whether expressivism about any particular class of terms is correct. Baker and Woods (2015) discuss further natural examples of B-type inconsistencies and conclude that they are no less familiar than A-type inconsistencies. May the expressivist, therefore, turn the negation problem on its head? We are inclined to take the inconsistency of *Murdering is legal* and *Murdering is not legal* to display the inconsistency-transmitting property of belief. The expressivist might claim that the very data constituting the negation problem show (i) that *Murdering is wrong* and *Murdering is not wrong* express different types of attitude, and (ii) that these attitudes are B-type inconsistent. Unfortunately for the expressivist, this will not do. At least the following problems remain.

The compositional problem. The contrast between (1) and (3) brings to light the *compositional* version of the negation problem. For these examples appear to show that expressivism requires two types of sentential negation: an A-type negation that operates on *contents*, like the *not* in (3b), and a B-type negation that operates on *attitudes*, like the *not* of (1b). This division however is not reflected in language—there are no *A-not* or *B-not* realised as distinct lexical items. Thus, in order to give a compositional semantics, one should give a uniform analysis of the particle *not* as a compositional operator. It is unclear at this point how the expressivist could do this. It is also a mistake to stipulate an *ambiguity* of the word ‘not’ to two distinct operators *not_A* and *not_B*. In *murdering is not wrong*, the B-reading is mandatory and the A-reading is not available. If an ambiguity is postulated, the unavailability of the A-type reading is still in need of explanation.

The logicity problem. We have observed that *murdering is wrong* and *murdering is not wrong* sound inconsistent, but we have been using the term ‘inconsistency’ quite loosely. But *murdering is wrong* and *murdering is not wrong* are inconsistent in a formally precise way: they are *logically* inconsistent, meaning that it is sufficient to understand the meaning of *not* to recognise them as inconsistent; one may be entirely ignorant about the meaning of *murdering* or *wrong*. This is in contrast to *factual* inconsistencies, like *grass is green and grass is blue* or *murdering is wrong and murdering is right*. To recognise these as inconsistent, one needs additional knowledge of the non-logical vocabulary featuring in them. However, the rough expressivist explanation of the relevant inconsistency rests on the recognition that *not* modifies the attitude expressed by *wrong* and that *not* does not modify attitude in every context. So it seems that some understanding of *wrong*—at least that it *is* an attitude expression—is required to recognise the inconsistency of *Murdering is wrong* and *Murdering is not wrong*, contravening logicity.

The explanatory problem. The expressivist has made the following assumptions: (i) there are B-type inconsistencies; (ii) for each attitude whose expression is linguistically realised (e.g. *wrong* realising the expression of *disapproval*) there is another attitude (e.g. *tolerance*) that may not be linguistically realised; (iii) all these attitudes stand in appropriate logical relations

to one another (e.g. disapproval and tolerance towards the same act are B-type inconsistent). Taken together, these assumptions commit the expressivist to the existence of a set of attitudes (not all of which need to be linguistically realised) that stand in a reasonably complex *web* of logical relations. The expressivist cannot just assume that this web exists, but must explain where it comes from.

An account that must contend with the explanatory problem is due to Terence Horgan and Mark Timmons (2006). They construct a language for *logically complex* attitude expressions, starting with two basic sentence-forming operators to express descriptive is-commitment and normative ought-commitment, respectively. They then recursively define logical connectives on these operators, e.g. that for each operator there is another one that negates it. The meanings of these complex operators are given by their inferential role. However, Schroeder (2008a) incisively points out, commitments (or attitudes) cannot themselves be logically complex—only the language that Horgan and Timmons use to describe these commitments is logically complex. But a logically complex language might simply be overwrought and does not in itself guarantee that its expressions denote anything, so Horgan and Timmons have yet to explain why we should suppose the attitudes their language requires exist.

3 Inferential expressivism

3.1 A first pass

Inferential expressivism is an approach to meaning that combines aspects of expressivism and inferentialism. As mentioned, *expressivism* is the view on which the meaning of a linguistic term derives from the attitude it is used to express. *Inferentialism* is the view that the meaning of a term is given by its inferential role—that is, by when one can infer sentences containing the term, and what follows from such sentences. For example, inferentialists claim that the following *rules of inference* characterise the meaning of conjunction (Gentzen, 1935; Prawitz, 1965).

- From A and B infer $A \wedge B$.

- From $A \wedge B$ infer A .
- From $A \wedge B$ infer B .

We will write such inference rules in a natural deduction calculus. In this notation, the following rules for *conjunction introduction* and *conjunction elimination* define the meaning of \wedge .

$$(\wedge I.) \frac{A \quad B}{(A \wedge B)} \quad (\wedge E.1) \frac{(A \wedge B)}{A} \quad (\wedge E.2) \frac{(A \wedge B)}{B}$$

Expressivism and inferentialism share an intellectual heritage. Both are motivated by supposing that, in some sense, *meaning is use*. Expressivism holds that the expression of certain attitudes is central to how a term is used (Gibbard, 2003). Inferentialists claim that inferential roles best characterise use (Dummett, 1991; Brandom, 1994). Inferential expressivism combines these views by specifying the meaning of an expression in terms of *the attitudes* one can *infer* from the use of sentences that contain that expression (Chrisman, 2008; Incurvati and Schlöder, Forthcoming).

Let's start with the attitude of *assent*. For brevity—and following Rumfitt (2000)—write $+A$ for the expression of assent to the proposition A . Then, the inferential expressivist meaning for conjunction is given by the following rules:

$$(+\wedge I.) \frac{+A \quad +B}{+(A \wedge B)} \quad (+\wedge E.1) \frac{+(A \wedge B)}{+A} \quad (+\wedge E.2) \frac{+(A \wedge B)}{+B}$$

That is, from the expression of assent to $A \wedge B$, one can infer assent to A and assent to B (and *vice versa*). At first, that may seem like an odd notion of inference. Indeed, as noted by Greg Restall (2005) there is a mind-cluttering problem here (see also Harman, 1986). Since arbitrarily many propositions follow from any proposition A ($A \wedge A$, $A \wedge A \wedge A$, ...), inferential expressivism seems to entail that anyone who assents to a single proposition assents to an unbounded number of propositions. This is cognitively implausible, so the inferential expressivist needs to be more precise about what she means. The proper understanding of *inferred assent* here is *social*: the meaning-conferring rules define which attitudes one is *committed* to have (see also Dutilh Novaes, 2015; Incurvati and Schlöder, 2017). For instance, given $(+\wedge I.)$, someone who explicitly assents to A and to B may not be in a mental state that includes assent to $A \wedge B$

(since she may fail to draw the inference corresponding to $(+\wedge I)$). Rather, she is *committed* to assenting to $A \wedge B$, since if the inference is pointed out to her, she must assent to $A \wedge B$ or admit to a mistake.

The advantages of inferential expressivism can be appreciated by considering the case of negation. Traditional expressivism takes the connection between a term receiving expressivist treatment and the attitude it expresses to be *direct*: the term itself expresses an attitude (Ayer, 1936; Stevenson, 1937). Thus, traditional expressivism about negation holds that *not* expresses an attitude; call it *dissent*. Inferential expressivism, by contrast, takes the relation between negation and the expression of dissent to be *inferential*. That is, *not* does not directly express dissent, but from the use of a sentence containing a negation as the main operator one can *infer* that the speaker dissents. Such accounts of negation have been developed within the *bilateral programme* in the philosophy of logic (Smiley, 1996; Rumfitt, 2000; Incurvati and Schlöder, 2017) and we now show how these accounts can be regarded as a special case of inferential expressivism.

3.2 Bilateralism and inferential expressivism about negation

Gottlob Frege (1919) argued that rejecting a proposition is the same as asserting its negation. Towards a *reductio*—in what is known as the Frege–Geach argument—he supposes that *not* is a speech-act marker for rejection. He then notes the following valid inference.

- (4) a. If not p , then not q .
 b. Not p .
 c. Not q .

Frege points out that the *not p* in (4a) cannot be a rejection of p , since somebody uttering (4a) might assent to p . Thus, the *not* in (4a) must *modify* the proposition p (instead of indicating a speech act *about* it). Suppose we nevertheless insist that in unembedded contexts such as (4b) *not p* is a speech-act marker for rejection. Then, (4b) is a rejection of p . But this means that (4b) does not coincide with the antecedent of (4a), and so (4) cannot be validated by *modus ponens*. For the inference to be an instance of *modus ponens*, the *not* in (4b) must modify p . But then *not* does not indicate rejection.

As pointed out by Timothy Smiley (1996), while the Frege–Geach problem does show that *not* should not be analysed as indicating rejection, this does not mean that one cannot *explain* negation by *appealing* to the speech act of rejection. Smiley points out that there is an independent and non-embeddable way of indicating rejection. To wit, posing a polar question to oneself and answering negatively performs a rejection. Similarly, answering positively performs an assertion.

- (5) a. Is it [the case that] p ? Yes! *asserts p*
 b. Is it [the case that] p ? No! *rejects p*

Smiley notes that these speech acts can figure in inferences. In particular, he draws attention to inferences such as (6).

- (6) a. Is it the case that, if q , then p ? Yes!
 b. Is it the case that p ? No!

 c. Is it the case that q ? No!

One might claim that *Is it the case that p? No!* is simply a different way of asserting *It is not the case that p* and analyse (6) as *modus tollens*. However, Smiley notes, one can recognise (6) as valid without theorising about the nature of negation at all. Roughly, someone uttering (6a,b) cannot assert q on pain of being inconsistent: asserting q would entail p by (6a) and the standard semantics of the conditional, which is inconsistent with the rejection of p in (6b). By virtue of being unable to (consistently) assert q , she is committed to reject q (6c). This reasoning did not make any mention of negation. Similarly, we may consider an inference similar to (4), but where we make explicit that the minor premiss and conclusion are rejections.

- (7) a. Is it the case that, if not p , then not q ? Yes!
 b. Is it the case that p ? No!

 c. Is it the case that q ? No!

But now we have a puzzle. The speech act indicators (5) that Smiley postulates are non-embeddable—*if is it the case that p? No!, then...* borders on incomprehensible—but as shown by (6) and (7) they can nonetheless feature in inferences. To simply reduce *not p* to *Is it p?*

No! seems unsatisfactory due to the divergent embedding behaviour of these phrases (Rumfitt, 2000). But if (7b) is not reducible to the antecedent of (7a), then—following the structure of the Frege–Geach argument—how can (7) be valid?

Classically conceived, propositional logic considers only asserted content (Frege, 1879). However, based on the above arguments, Smiley (1996) concludes that the best explanation of *all* the data—including (6) and (7)—distinguishes two kinds of content: asserted and rejected. Thus, logic should be *bilateral*, i.e. defined in terms of both assertion and rejection. The bilateralist logician takes *Is it p? No!* to be an (unembeddable) speech-act indicator and *not* to be an (embeddable) compositional operator that is appropriately related to the speech act of rejection. Relations of this kind should, among other things, explain the validity of inferences like (7). Earlier work by Ian Rumfitt (2000) and ourselves (Incurvati and Schlöder, 2017) specifies these relations to be *inferential* and takes them to be *constitutive* (i.e. meaning-conferring) of the negation connective.

This can be seen as an inferential expressivist account of negation. First, we may suppose that speech acts are expressions of attitudes; call the attitude expressed by assertion *assent* and the attitude expressed by rejection *dissent*. (This should come as an entirely natural step in the context of the Frege–Geach debate: Frege’s arguments about speech acts are typically thought of as arguments about attitude expressions.) Following Smiley, we can hence consider answers to self-posed polar questions to be non-embeddable expressions of attitude.

- (8) a. Is it [the case that] *p*? Yes! *asserts p* and thereby *expresses assent to p*
 b. Is it [the case that] *p*? No! *rejects p* and thereby *expresses dissent from p*

Then, Rumfitt (2000) proposes the following inferences to be (part of) the meaning of negation:

- (i) From assent to a negated proposition, one can infer dissent from the bare proposition; and
 (ii) from assent to a proposition, one can infer dissent from its negation. Again writing + for assent and now \ominus for dissent, we can state these inferences as follows.

$$(+\neg\text{E.}) \frac{+\neg A}{\ominus A} \quad (\ominus\neg\text{I.}) \frac{+A}{\ominus\neg A}$$

According to inferential expressivism, these rules (partially) constitute the meaning of negation: they state which attitudes one can infer from attitudes towards negated propositions, and

from which attitudes one can infer (other) attitudes about negated propositions. For instance, uttering *Murdering is not legal* according to the bilateralist expresses assent to the proposition $\neg\text{legal}(m)$. The meaning of this proposition is given by the inferential roles of its constituents; in particular the role of \neg , which is stated in terms of both assertion and rejection. Part of this meaning is that from assent to $\neg\text{legal}(m)$ one can infer dissent from $\text{legal}(m)$ per $(+\neg\text{E.})$. This is in contrast to traditional expressivism about *not* that holds that uttering *Murdering is not legal* would *directly* express dissent from $\text{legal}(m)$.

The precise statement of the meaning-conferring rules for negation varies across the literature; compare, e.g., Rumfitt (2000), Francez (2014) and Incurvati and Schlöder (2017). We elaborate our preferred rules further below. Taking negation to have these rules, however, is not sufficient to explain all the data considered above. The bilateralist also needs *coördination principles* governing the interaction between assent and dissent (or between assertion and rejection). Following Smiley (1996) and Rumfitt (2000), we adopt the following *Smileian reductio* principles.

$$\text{(Rejection)} \frac{+A \quad \ominus A}{\perp} \quad \text{(SR}_1\text{)} \frac{\begin{array}{c} [+A] \\ \vdots \\ \perp \end{array}}{\ominus A} \quad \text{(SR}_2\text{)} \frac{\begin{array}{c} [\ominus A] \\ \vdots \\ \perp \end{array}}{+A}$$

These rules define assent and dissent to be contrary attitudes: (Rejection) states that it is inconsistent to assent to and dissent from the same proposition;⁴ the (SR)'s state that whenever it is inconsistent to hold one attitude towards some content, one is committed to hold the other one.⁵ Together with bilateral *modus ponens*—the rule for conditional elimination $(+\rightarrow\text{E.})$ —this suffices to explain Smiley's inference (6): if (6a) $+q \rightarrow p$ and (6b) $\ominus p$, then the supposition $+p$ entails \perp by *modus ponens* and (Rejection). Smileian *reductio*₁ then allows us to infer (6c) $\ominus p$.

⁴This does not mean that one *cannot* simultaneously assent to and dissent from the same proposition (for example, one can compartmentalise). Rather, the relevant sense of inconsistency here is that two attitude expressions are inconsistent when they result in a communicative breakdown (Baker and Woods, 2015, p414).

⁵Smiley (1996) and Rumfitt (2000) do not consider these principles to be in need of further justification, but linguistic and conceptual evidence for their validity is given in Francez (2014) and Incurvati and Schlöder (2017).

$$(+ \rightarrow E.) \frac{+(A \rightarrow B) \quad +A}{+B}$$

Bilateralism—as a form of inferential expressivism—succeeds in meeting the (original) Frege–Geach challenge head on. Bilateralists agree with Frege that attitude expressions do not embed: the attitude expressions in (8) are linguistically unembeddable and the signs $+$ and \ominus *decorate* formulae and hence cannot embed either. Bilateralists also accept Frege’s conclusion that, as a result, *not* cannot be an attitude expression, since it embeds. But, they continue, this does not mean that the meaning of *not* cannot be explained by appealing to the attitude of dissent. The general semantic framework of inferential expressivism makes clear what kind of meanings bilateralists are proposing for negation: they explain *not* by stating which attitudes one can infer from the use of *not*.

However, the bilateralist strategy to explain negation raises a question. Bilateralists seem to uncritically take as basic two attitudes and stipulate them to stand in a B-type inconsistency relation to one another (per the Smileian *reductio* rules). Does bilateralism therefore fall prey to the negation version of the Frege–Geach problem?

3.3 Bilateralism and the negation problem

Bilateralists take it as primitive that it is inconsistent to simultaneously assent to and dissent from the same proposition. Some may object that this already falls prey to the negation problem: the bilateralist owes an explanation of *why* these attitudes are inconsistent. But this objection is unfair.

It should be uncontroversial that one needs to take *some* basic type of inconsistency as primitive. Schroeder (2008a) posits as basic (i) the familiar truth-conditional inconsistency between a proposition and its negation; and (ii) the fact that some attitudes (such as belief and intent) are *inconsistency-transmitting*. The A-type inconsistency of *believing that p and believing that not p* follows from *p and not p* being truth-conditionally inconsistent and from this inconsistency being *transmitted* to the level of belief. The bilateralist, by contrast, posits as basic (i) the B-type inconsistency of assent and dissent; and (ii) that negation is explained by its inferential relation to the expression of dissent. This explains the supposedly A-type inconsistency of *believing that p and believing that not p* by noting that someone who believes

that p must *assent to* p , and someone who believes that *not* p must *dissent from* p —and it is inconsistent to both assent and dissent from p .

Abstracting from there, we can say that there are *A-type expressivists* like Schroeder (2008a) who posit A-type inconsistency as basic and attempt to reduce apparent B-type inconsistencies to A-type.⁶ But on the other side of the aisle there are the bilateralists, who take B-type inconsistency as basic and attempt to reduce apparent A-type inconsistencies to B-type. Both groups need to take some kind of inconsistency as basic and use it to explain the other one.

The A-type expressivist might further demand an explanation of the bilateralist of *why* assent and dissent are inconsistent—supposedly, asking the bilateralist to provide some fundamental property of the mind that would entail this inconsistency. But the bilateralist might equally demand an explanation of why some attitudes are inconsistency-transmitting—asking the A-type expressivist to name the underlying reason that explains why *belief* transmits inconsistencies, but *wonder* does not. So in terms of explanatory credentials, A-type expressivism and bilateralism are on equal footing.

To be sure, the negation problem we discussed in Section 2 is not thereby solved. Both A-type expressivists and bilateralists still need to explain compositionality and logicity. In addition, the bilateralist has not yet provided a semantics for *wrong*. At this stage, we are merely defending the starting point of bilateralism—that there are two attitudes we may call *assent* and *dissent* that stand in a B-type inconsistency relation—against the charge of being unexplanatory.

Also, we do not claim that the whole of the explanatory challenge is unfair. Those expressivists like Horgan and Timmons (2006) that have logical operators such as negation *generating* new operators for attitude expressions are fairly challenged with having to explain what these attitudes are and why they have the required logical properties. But the bilateralist does not do anything like this. Horgan and Timmons claim that a logical complex sentence expresses a lo-

⁶Schroeder (2008a) himself explains the apparent B-type inconsistency between *Murdering is wrong* and *Murdering is not wrong* as the A-type inconsistency between *being for blaming for murdering* and *being for not blaming for murdering*, stipulating that *being for* is an inconsistency-transmitting attitude. We discuss this further in Section 4.

gically complex attitude; the meaning of this attitude, they continue, is defined by its inferential role. The bilateralists agree with Schroeder (2008a) that there are no logically complex attitudes. They state the meanings of attitude expressions as inferential roles, but the complexity lies with the contents of those attitudes. To wit, the bilateralist deals in *simple* attitudes (assent or dissent), held *towards* logically complex *propositions*. Furthermore, the two basic attitudes of the bilateralists and their logical properties (given by Smileian *reductio*) are linguistically observable (instead of being generated by logical vocabulary). While Horgan and Timmons (and others) do have an explanatory problem, the bilateralists do not.

Schroeder (2008a) nevertheless considers A-type expressivism superior, since ‘B-type inconsistency is not something that expressivists can take for granted, because there are no good examples of it’ (p48). However, there *are* natural examples of attitudes that stand in a relation of B-type inconsistency, e.g. *belief* and *wonder*, or in other logical relations, e.g. *certainty* entails *belief*. Such attitudes and their logical relations are linguistically observable, and in terms of explanation are on a par with the observation that certain attitudes (like *belief*) are inconsistency-transmitting (Baker and Woods, 2015).

In sum, either there is no explanatory problem for the bilateralist or there is an analogous problem for the A-type expressivist. However, there is a serious explanatory challenge for expressivists that (i) take as basic attitudes and logical properties that are not observable, but are needed to make expressivist semantics work, or (ii) take *both* A-type and B-type inconsistency as basic. The bilateralist does neither. Both assent and dissent, as well as their logical properties, are linguistically observable by examining the speech acts of assertion and rejection. And A-type inconsistency is explained in terms of B-type inconsistency.

The bilateralist still needs to address the aspects of the negation problem related to compositionality and logicity and to include normative vocabulary in her account. To this end, we show how bilateral semantics can be extended to a *multilateral* semantics by taking further linguistically observable attitudes as primitive. We first present the inferential expressivist account of the epistemic modal *might*. This analysis of epistemic modals will be helpful in understanding the inferential expressivist account of *wrong* and in solving the *new new negation problem* in Section 4.

3.4 Inferential expressivism beyond negation

According to Smiley (1996), posing a polar question to oneself and answering it is one way of realising attitude expressions. He restricts attention to the answers *Yes!* and *No!*, but as we note in Incurvati and Schlöder (Forthcoming), there is a third possible answer: *Perhaps!*⁷ We call the speech act performed by answering *Perhaps!* to a polar question *weak assertion* and the attitude it expresses *weak assent*. As before, we mark assent with +, dissent with \ominus and now weak assent with \oplus .

- (9) a. Is it *p*? Yes! *asserts p* and thereby *expresses assent to p* (+*p*)
b. Is it *p*? No! *rejects p* and thereby *expresses dissent from p* ($\ominus p$)
c. Is it *p*? Perhaps! *weakly asserts p* and thereby *expresses weak assent from p* ($\oplus p$)

But how should we characterise these speech acts? Stalnaker (1978) famously argued that the essential effect of an assertion is a proposal to add a proposition to the common ground (or to accept such a proposal).⁸ Within this framework, it is natural to take the essential effect of a rejection as that of marking a proposition as *not being accepted* in the common ground because the speaker dissents from it. This means that rejections can be *weak* (Dickie, 2010; Incurvati and Schlöder, 2017): asserting *not p* may be stronger than rejecting *p*, since there are circumstances where one may dissent from a proposition and its negation. The following is a natural example:

(10) *Alice*: X or Y will win the election.

Bob: Is it the case that X or Y will win? No! X or Y or Z will win.

Bob is here dissenting from $\lceil X \text{ or } Y \text{ will win} \rceil$, as is expressed by the particle *no*. But it would be a mistake to read Bob's rejection as expressing assent to $\lceil \textit{it is not the case that X or Y will} \rceil$

⁷There is linguistic evidence for *perhaps* being a force-indicator similar to *Yes!* and *No!* (Incurvati and Schlöder, Forthcoming). Notably, *perhaps* does not embed in e.g. the antecedents of conditionals (*#if perhaps it is raining,...*), exactly as one would expect of a force indicator.

⁸The widespread view that an assertion immediately results in the addition of a proposition to the common ground is based on a misreading of Stalnaker. He is explicit that addition to the common ground is pending acceptance (1978, fn. 9) and we agree.

win⌋, since this would entail that he assents to ⌈*neither X nor Y will win*⌋. But it seems that Bob is dissenting from that proposition as well—he leaves open who wins.

What about weak assertion? We take this speech act to have the essential effect of rejecting a negative (see Incurvati and Schlöder, Forthcoming for details). Consider again (10). While dissent from ⌈*X or Y will win*⌋ is part of the content of Bob’s utterance, dissent from ⌈*neither X nor Y will win*⌋ is merely *conveyed* via a pragmatic implicature: if Bob had not intended to dissent from ⌈*neither X nor Y will win*⌋, he would have explicitly assented to ⌈*Z will win*⌋. Indeed, this implicature can be cancelled.

(11) *Alice*: *X or Y will win the election.*

Bob: Is it the case that *X or Y will win*? No! *X or Y or Z will win*. In fact, *Z will*.

As we argue in Incurvati and Schlöder (Forthcoming), *weak assertion* is the mechanism by which Bob can *explicitly* express dissent from ⌈*neither X nor Y will win*⌋ here. Compare (12), where this effect of uttering *perhaps*—that one is dissenting from ⌈*neither X nor Y will win*⌋—is non-cancellable.

(12) Is it the case that *X or Y will win*? Perhaps! #In fact, neither of them will.

Thus, weakly asserting *X or Y will win* by way of answering *Perhaps!* rejects the negative of ⌈*X or Y will win*⌋ (and nothing more). By generalisation, this explains the following inference rules for negation.

$$\begin{array}{cc} (\ominus\text{-I.}) \frac{\oplus A}{\ominus \neg A} & (\ominus\text{-E.}) \frac{\ominus \neg A}{\oplus A} \\ (\oplus\text{-I.}) \frac{\ominus A}{\oplus \neg A} & (\oplus\text{-E.}) \frac{\oplus \neg A}{\ominus A} \end{array}$$

That is, if one dissents from a negative, one is committed to weakly assent to the non-negated proposition and *vice versa*. And if one weakly assents to a negative, one is committed to dissent from the non-negated proposition and *vice versa*. According to inferential expressivism, these rules are *meaning-conferring* for the negation operator.

Now, as we show in Incurvati and Schlöder (Forthcoming), one can similarly give rules that define the meaning of the epistemic modal *might* (formalised as \diamond). We cannot go into detail

here, but one can easily see that asserting *it might be that p* is inferentially equivalent to *Is it p? Perhaps!* and that *perhaps* iterates with *might*. Thus, the following rules give the meaning of epistemic modals.

$$\begin{array}{ll} (+\diamond I.) \frac{\oplus A}{+\diamond A} & (+\diamond E.) \frac{+\diamond A}{\oplus A} \\ (\oplus\diamond I.) \frac{\oplus A}{\oplus\diamond A} & (\oplus\diamond E.) \frac{\oplus\diamond A}{\oplus A} \end{array}$$

When we add the rules for epistemic modals, the following rules are derivable, which tell us how negation interacts with assent. Later, these rules will be useful to characterise the meaning of *murdering might be wrong* and to account for the distinction between an utterance of *Murdering is wrong* and *Murdering might be wrong*.

$$(+\neg I.) \frac{\ominus\diamond A}{+\neg A} \quad (+\neg E.) \frac{+\neg A}{\ominus\diamond A}$$

Since our semantics now is *multilateral* in that it takes more than two attitudes as basic, we need additional principles to coördinate assent and weak assent. These are the rules of (Assertion) and (Weak Inference).

$$\text{(Assertion)} \frac{+A}{\oplus A} \quad \text{(Weak Inference)} \frac{\begin{array}{c} [+A] \\ \vdots \\ +B \end{array} \oplus A}{\oplus B} \quad \text{if } (+\diamond E.) \text{ and } (\oplus\diamond E.) \text{ were not used to derive } +B \text{ and only } +\text{ed premisses occur in the derivation of } +B.$$

The justification of (Assertion) is straightforward: if someone assents to *A*, she cannot also assent to *not A* (*pace* paraconsistent logics), so she is committed to dissent from *not A*. The coördination principle (Weak Inference) is justified by the evident validity of inferences like (13):

- (13) a. Is it the case that if *A*, then *B*? Yes!
 b. Is it the case that *A*? Perhaps!
 c. Is it the case that *B*? Perhaps!

Like Smiley's *modus tollens*-like inference (6), (13) is a valid scheme that needs to be accounted for by the coördination of the fundamental attitudes. We justify the proof-theoretic restrictions of (Weak Inference) elsewhere (Incurvati and Schlöder, Forthcoming); they are related to issues

arising from weak attitudes interacting with conditionals in unexpected ways (Kolodny and MacFarlane, 2010; Incurvati and Schlöder, 2017).⁹

The expressive inferentialist approach to negation and epistemic modality has a number of desirable properties. Write \vdash^{EML} (Epistemic Multilateral Logic) for the proof theory containing all above inference rules. The resulting account then satisfies the following desiderata identified in the prior literature.¹⁰

- Classicality of assent: if $A \vdash B$ in classical logic, then $+A \vdash^{EML} +B$.
- Epistemic contradiction (Yalcin, 2007; Mandelkern, 2019): $+(A \wedge \diamond\neg A) \vdash^{EML} \perp$.
- Non-factive *might* (Russell and Hawthorne, 2016): $+\diamond A \not\vdash^{EML} +A$.
- Rejection/dissent is weak (Dickie, 2010): $\ominus A \not\vdash^{EML} +\neg A$.
- Negation entails dissent (Rumfitt, 2000): $+\neg A \vdash^{EML} \ominus A$ and $+A \vdash^{EML} \ominus\neg A$.

Epistemic Multilateral Logic is sound and complete with respect to an appropriate model theory and the calculus can be extended in a natural way to include quantifiers (Aloni et al., ms).

To sum up, we have an inferential expressivist account of *not* and *might* that takes as basic the attitudes of *assent*, *dissent* and *weak assent*. The relation between the attitudes is characterised by the coördination principles, and the meaning of *not* and *might* is constituted by the above rules for their introduction and elimination. As argued above for bilateralism, our multilateral account is not subject to the explanatory part of the negation problem. The fundamental attitudes we make use of are linguistically observable, as are the logical properties encoded as coördination principles. We now apply this framework to normative vocabulary.

⁹For the same reasons, this account of epistemic modals does not satisfy the conditional proof rule that from $+A$ entailing $+B$, one can infer $+A \rightarrow B$. Rather, one is only entitled to infer $+A \rightarrow B$ if the inference to $+B$ from $+A$ satisfies the restrictions on (Weak Inference).

¹⁰Some may believe the first three to be intrinsically incompatible, because $+(A \wedge \diamond\neg A) \rightarrow \perp$ classically entails $+\diamond A \vdash +A$. However, Epistemic contradiction does not entail $+(A \wedge \diamond\neg A) \rightarrow \perp$ because of the restrictions on the conditional proof rule.

3.5 Inferential expressivism about normative vocabulary

According to traditional expressivism, the semantic value of *wrong* is the expression of disapproval. According to inferential expressivism, the semantic value of *wrong* is that having the attitude of assent towards a proposition like $\lceil \textit{murdering is wrong} \rceil$ means that one can infer the attitude of disapproval towards $\lceil \textit{murdering} \rceil$. That is, as above for the terms *not* and *might*, the meaning of *wrong* is given by how attitudes towards propositions containing *wrong* inferentially interact with other attitudes towards different contents. In particular, the inferential expressivist meaning of *wrong* is given by the following rules of inference (writing \mathcal{D} for the attitude of disapproval).

$$(+WI.) \frac{\mathcal{D}a}{+wrong(a)} \qquad (+WE.) \frac{+wrong(a)}{\mathcal{D}a}$$

This semantics provides enough places to insert a negation, since *wrong* is treated as an embeddable predicate. The attitude expressed by uttering *Murdering is wrong* is $+wrong(m)$, the attitude expressed by *Not murdering is wrong* is $+wrong(\neg m)$ ¹¹

What does $+ \neg wrong(m)$ mean? The glib answer is that the meaning of this attitude expression is given by the inference rules that define the meaning of \neg and the rules that define the meaning of *wrong*.¹² This may be too glib to be satisfactory, so let us explore this inferential

¹¹To our knowledge, nobody in this debate has commented much on how one negates the logical form of subject gerunds like *murdering* (notably, Schroeder (2008a, p.73ff) relegates this question to a *logic of blaming* that he leaves open). We suppose that $wrong(\neg m)$ is a placeholder for a more complex first order formula. Linguistic evidence suggests that subject gerunds are quantificational (Portner, 1995), so, plausibly, $wrong(m)$ stands for $\forall x.act-of-murder(x) \rightarrow wrong(x)$. Some care is required to negate this, however. *Not murdering is wrong* should not entail that any non-murdering action is wrong, as this would mean that *everything except murder* is wrong. One could let $wrong(\neg m)$ stand for $\forall^D x. \neg act-of-murder(x) \rightarrow wrong(x)$ where the universal quantifier is restricted to a domain D that stems from a presupposed set of alternatives; alternatively, *not murdering* could be interpreted as a term negation, viz. $\forall x.act-of-un-murder(x) \rightarrow wrong(x)$. The former approach appears to be supported by linguistic evidence (Portner, 1995). We leave this matter open, but note that our semantics for negation and normative vocabulary would work for either.

¹²This, to stress, differentiates inferential expressivism from the proposal of Horgan and Timmons (2006): they describe the meaning of *Murdering is not wrong* as a logically complex attitude. We describe $\lceil \textit{Murdering is not wrong} \rceil$ as a logically complex proposition towards which one may have attitudes.

meaning.

First, $+\neg wrong(m)$ clearly entails $\ominus wrong(m)$, i.e. dissent from $\lceil murdering\ is\ wrong \rceil$. This means that the speaker is committed to disagree with any expression of disapproval of $\lceil murdering \rceil$. But dissent from $\lceil murdering\ is\ wrong \rceil$ is already entailed by assent to $\lceil murdering\ might\ not\ be\ wrong \rceil$ and there clearly is a difference between uttering *Murdering is not wrong* and *Murdering might not be wrong*. Indeed, $+\neg wrong(m)$ entails something stronger, namely $\ominus\Diamond wrong(m)$, i.e. dissent from $\lceil murder\ might\ be\ wrong \rceil$. But in what sense exactly is this stronger than dissent from $\lceil murder\ is\ wrong \rceil$? We can characterise $\ominus\Diamond wrong(m)$ attitude as a special kind of dissent from $\lceil murdering\ is\ wrong \rceil$. Namely, *stable* dissent.

The attitude of assent is *stable* in the sense that if one assents to a proposition p one cannot come to stop assenting to p by simply being provided additional information—it requires a change of mind to stop assenting (Restall, 2005). But, in general, if one dissents from p or weakly assents to p , one may come to change these attitudes *merely* by receiving additional information (Incurvati and Schlöder, 2017). The difference in stability can also be observed when considering the speech acts that are used to express these attitudes.

(14) *Alice*: X or Y will win the election.

Bob: Is it the case that X or Y will win? No! X or Y or Z will win.

As argued above, the essential effects of our three speech acts are as follows: an assertion puts forward a proposal to accept a proposition into common ground; a rejection marks a proposition as not being accepted into common ground; and a weak assertion rejects a negative. Assertion is stable in the sense that once a proposition is in the common ground, it remains in it unless the common ground is revised. A rejection, however, is unstable in that a previously rejected proposition can become common ground simply because other, new information is added to the common ground and hence *without any revision of the common ground*.

(14) is an example of this phenomenon: Bob's utterance marks $\lceil X\ or\ Y\ will\ win \rceil$ as unaccepted into the common ground. But if the proposition $\lceil X\ or\ Y\ or\ Z\ will\ win \rceil$ asserted by Bob does become common ground and later Alice and Bob add $\lceil Z\ dropped\ out \rceil$ to the common ground as well, $\lceil X\ or\ Y\ will\ win \rceil$ will enter the common ground after all, but without any revision of the common ground. Hence, Bob's rejection of $\lceil X\ or\ Y\ will\ win \rceil$ was unstable, as

undoing it required no revision. The case for weak assertion being unstable is analogous.

Thus, our account has the resources to distinguish between saying *Murdering is not wrong* and *Murdering might not be wrong*. By uttering either sentence, the speaker can express dissent from the proposition $\lceil \textit{murdering is wrong} \rceil$. However, uttering *murdering is not wrong* expresses stable dissent (i.e. changing this attitude would be a change of mind), whereas uttering *Murdering might not be wrong* expresses unstable dissent—the speaker may come to express something else about *murdering* without changing their mind, simply by receiving additional information. The formal expression of stable dissent from a proposition p is $\ominus\Diamond p$, which is inferentially equivalent to $+\neg p$. Thus, the inferential meaning of $\lceil \textit{murdering is not wrong} \rceil$ is the expression of stable dissent from $\lceil \textit{murdering is wrong} \rceil$.

Note that we did not introduce an auxiliary attitude (such as *tolerance*) to account for what is expressed by uttering *Murdering is not wrong*—we only need the three foundational attitudes of expressive inferentialism together with the attitude of *disapproval*. If someone wishes to call the attitude expressed by $\ominus\Diamond \textit{wrong}(m)$ by the name *tolerance of murder*, she can do so—and this may be a useful and illuminating shorthand. But *only* a shorthand. The inferential expressivist does not need to take the attitude of tolerance as a primitive.

In sum, inferential expressivism solves the negation problem for expressivism about *wrong*. The aspects of compositionality and logicity are accounted for by the fact that inferential expressivism posits the same negation operator for descriptive and normative language. The explanatory problem is avoided by not stipulating any auxiliary or complex attitudes, instead explaining the meaning of *Murdering is not wrong* by appealing to the joint inferential meaning of *not* and *wrong*.

The account straightforwardly generalises to further normative vocabulary like *right*. Supposedly, traditional expressivism takes *right* to be the expression of *approval*. Hence, according to inferential expressivism, the semantics of *right* is such that one can *infer* approval from assent to a sentence containing *right*. That is, the meaning of *right* is given by the following rules (writing \mathcal{A} for the attitude of approval).

$$(+RI.) \frac{\mathcal{A} a}{+\textit{right}(a)} \qquad (+RE.) \frac{+\textit{right}(a)}{\mathcal{A} a}$$

The meaning of sentences like *Murdering is not right* is then explained analogously to the

above explanations of *Murdering is not wrong*. However, there is now one more inconsistency to address: the factual inconsistency of *Murdering is wrong* and *Murdering is right*. To derive this, we need to add an axiom encoding the inconsistency:

$$\text{(RW-contradiction)} \quad + \neg(\text{right}(a) \wedge \text{wrong}(a))$$

It is then immediate to derive the desired inconsistency. Note that (RW-contradiction) is not a coördination principle expressing fundamental properties of primitive attitudes, but an axiom expressing lexical knowledge about *right* and *wrong*. This is because the inconsistency of *Murdering is wrong* and *Murdering is right* is not logical, but relies on additional lexical knowledge.

4 The new and new new negation problems

4.1 Schroeder on the negation problem

Schroeder (2008a) defends an A-type account of *wrong*. Instead of analysing the attitude expressed by *wrong* as *disapproval*, he analyses it as *being for blaming for*, stipulating *being for* as his only primitive attitude. This allows him to insert a negation in the right place: *Murdering is not wrong* is analysed as *being for* \lceil not blaming for murdering \rceil . Then Schroeder claims that *being for* is an inconsistency-transmitting attitude (like belief), thereby accounting for all relevant data. This is remarkably elegant, but Schroeder himself notes some issues.

Notably, he acknowledges the *new negation problem* (NNP) that arises as a revenge version of the compositionality problem. It goes as follows. To give a uniform semantics—including both descriptive and normative vocabulary—that is grounded in the basic attitude of *being for*, Schroeder analyses descriptive claims as *being for proceeding as if* (short, *being for pai*) expressions, e.g. *Murdering is legal* expresses the attitude *being for* \lceil pai murdering is legal \rceil . But then, note the following.

NNP. According to Schroeder, *Murdering is wrong* expresses *being for* \lceil blaming for murdering \rceil and *Murdering is legal* expresses *being for* \lceil pai murdering is legal \rceil . Then, if *Murdering*

is not wrong expresses *being for* \lceil not blaming for murdering \rceil and the compositional semantics of *not* is uniform (as it should), the meaning of *Murdering is not legal* would be *being for* \lceil not pai murdering is legal \rceil . But this is a mistake: the attitude expressed by *Murdering is not legal* should be *being for* \lceil pai murdering is not legal \rceil .

In essence, the negation problem is that for normative language there is one space for a negation missing. The new negation problem is that for descriptive language, Schroeder has one space *too many* to put a negation.

To solve (NNP), Schroeder introduces the notion of a *biforcated* attitude. A biforcation is a pair of two *being for* attitudes such that the *major attitude* entails the *minor* one.¹³ We write biforcations as tuples and treat the left hand-side of a tuple to be the major attitude. What exactly the minor attitude is is determined by the lexical semantics of the relevant predicates; for descriptive vocabulary, one obtains the minor attitude from the major one by inserting two negations such that, e.g., the biforcated attitude expressed by *Murdering is legal* is \langle *being for* \lceil pai murdering is legal \rceil , *being for* \lceil not pai murdering is not legal \rceil \rangle , where *being for* \lceil pai murdering is legal \rceil is the major attitude (Schroeder, 2008a, p98)

Using such biforcations, Schroeder defines the meaning of negation as follows: the negation of a biforcation inserts in both the minor and major attitude a *not* between *being for* and the embedded action term and then *switches* major and minor attitude. That is, the following is Schroeder's compositional semantics for *not* (2008a, p106).

$$\llbracket \text{not} \rrbracket (\langle \text{being for } a, \text{ being for } b \rangle) = \langle \text{being for } \neg b, \text{ being for } \neg a \rangle$$

Thus, for instance, if a descriptive sentence *A* expresses the biforcation \langle *being for* \lceil pai *A* \rceil , *being for* \lceil \neg pai \neg *A* \rceil \rangle , then *not A* expresses \langle *being for* \lceil \neg pai \neg *A* \rceil , *being for* \lceil \neg pai *A* \rceil \rangle . Deleting double negations, one obtains the desired major attitude *being for* \lceil pai \neg *A* \rceil .

However, Schroeder now needs to insist that for *normative* propositions, the minor and major attitudes in a biforcation are identical, lest he run into the original negation problem again. For descriptive language, in contrast, the minor attitude is strictly weaker than the major one.

¹³The term 'biforcated' is Schroeder's, a pun on 'bifurcated' and 'being for'.

This is not an *ad hoc* move, but part of Schroeder’s strategy: by encoding a difference between the attitudes expressed by descriptive and normative terms on the level of lexical semantics, he is able to maintain uniform compositional semantics for negation while solving both the negation problem and the new negation problem. As a matter of fact, we agree that lexical semantics is the (only) right place to locate this difference.

Unfortunately, this move leads to the *new new negation problem* (Schroeder, 2008a, p113). Schroeder justifies his introduction of minor attitudes by appealing to a notion called *disacceptance*, which consists in not agreeing with a proposition without agreeing to its negation. Formally, on Schroeder’s account, to disaccept *A* is to accept the minor attitude in the biforcation expressed by *not A*. But since normative vocabulary sentences express biforcations with identical major and minor attitudes, the distinction between disacceptance and acceptance of a negative collapses for normative sentences. This entails that one cannot withhold judgement about an act *X* by disaccepting both ‘*X is wrong*’ and ‘*X is not wrong*’. The new new negation problem means that the only way to withhold judgement is to *not express* an attitude. Schroeder notes that this is not an *outright* bad result, concluding that it might be ‘a bullet to bite’ (p115).

However, this bullet becomes much harder to bite when also considering epistemic *might*. Schroeder suggests the following semantics for epistemic modals (p181): *might* deletes the major attitude and replaces it with the minor attitude. That is, his semantics for *might* is as follows.

$$\llbracket \textit{might} \rrbracket (\langle \textit{being for } a, \textit{ being for } b \rangle) = \langle \textit{being for } b, \textit{ being for } b \rangle$$

But given Schroeder’s solution to (NNP), this means that *Murdering might be wrong* expresses the same attitude as *Murdering is wrong*, since *Murdering is wrong* expresses a biforcation where minor and major attitude are the same. Schroeder (2008a, p182) concludes that hence either his semantics for *might* or his identification of minor and major attitudes for normative vocabulary must be revised. But no suitable such revision is in sight. The above semantics for *might* has compelling features, as Schroeder himself notes. To preserve these, and to also make sense of normative vocabulary under epistemic modality, Schroeder would very likely need to revise the foundations of the biforcated attitude framework. However, it is not clear whether it is possible to revise the framework in such a way as to solve both the original negation problem

and the new negation problem.

4.2 Inferential expressivism and the new new negation problem

There are some remarkable structural similarities between our approach and Schroeder's. His appeal to *disacceptance* roughly corresponds to our *dissent* and if *being for pai* is understood to be roughly like our *assent*, his minor attitudes are roughly like our *weak assent*, so his treatment of *might* is also similar to ours. But the expressive inferentialist account differs in that it sees no fundamental difference in how these attitudes operate on normative *vis-à-vis* descriptive vocabulary: we do not collapse assent with weak assent anywhere, whereas Schroeder collapses major and minor attitudes towards normative content. Accordingly, inferential expressivism makes a distinction between sentences like *Murdering might be wrong* and *Murdering is wrong*, solving the new new negation problem.

Now recall that to assert *Murdering is not legal* according to inferential expressivism is to propose the addition of the proposition $\neg legal(m)$ to the common ground. Since the common ground records the tacit assumptions in a conversation, this may indeed be paraphrased as *being for* $\lceil proceeding as if \neg legal(m) \rceil$. Analogously, to assert *Murdering is not wrong* it to propose the addition of $\neg wrong(m)$ to the common ground, which—by the inferential semantics of *not* and *wrong*—is to modify the common ground so that disapproval of murdering is stably ruled out. This can indeed be roughly paraphrased as *being for* $\lceil not blaming for murdering \rceil$. Thus, inferential expressivism, as developed in Section 3 can be examined in Schroeder's terms. Doing so shows no trace of the new negation problem. Due to the inferential expressivist treatment of *might*, the new new negation problem does not occur either. But why is that? Where does inferential expressivism draw the line that Schroeder draws when attributing different minor attitudes to descriptive and normative vocabulary?

Inferential expressivism locates this difference in whether meaning-conferring inference rules *change attitude*. The semantics of descriptive vocabulary is given by rules which do not change attitude, such as *from assent to X, infer assent to Y* (e.g. the meaning of *bachelor* includes that from assent to $\lceil John is a bachelor \rceil$ one may infer assent to $\lceil John is unmarried \rceil$). The semantics of normative vocabulary is given by rules which *do* change attitude. For in-

stance, *wrong* switches between assent and disapproval. This is why if one negates *wrong*, it may appear that one negates an attitude (namely, disapproval, the attitude *wrong* switches with), whereas this is not so when negating a descriptive term. Like Schroeder, we locate the difference between normative and descriptive vocabulary at the level of lexical semantics, and in particular in the way the rules of inferences constituting this semantics characterise the interaction of these terms with attitudes. This allows us to have uniform semantics for operators such as negation. Unlike Schroeder, we do not need to collapse any of our notions to do so.

5 Conclusion

We have argued that bilateralism is best understood as a form of inferential expressivism about negation: the meaning of negation is given in terms of its *inferential* connections to the *expression* of certain attitudes. Crucially, bilateralists make use of at least two distinct attitudes, assent and dissent, which they *coördinate* to stand in particular relations. Smiley (1996) argued that this move solves the original version of the Frege–Geach problem. We have demonstrated that this move also solves its negation version. In particular, bilateralism is not subject to the explanatory aspect of the negation problem, since its foundational assumptions are on a par with the assumptions made by *A-type* expressivists that certain attitudes transmit the inconsistency of truth and falsity.

Previous work of ours has extended inferential expressivism to a *multilateral* semantics which also accounts for the meaning of epistemic modals. In this paper, we have further expanded inferential expressivism so as to encompass moral vocabulary such as *wrong*. Thus, according to inferential expressivism about moral vocabulary, the meaning of *wrong* is given in terms of its inferential connections with the attitude of disapproval.

The following is an oft-told story about the metaethical landscape. Ethical cognitivism takes moral sentences to express beliefs but, unlike expressivism, has difficulty in explaining the motivating power of moral judgments. Traditional ethical expressivism takes moral sentences to express non-cognitive attitudes, but, unlike cognitivism, falls prey to the Frege–Geach problem. Hybrid approaches (see, e.g., Copp, 2001; Barker, 2002; Boisvert, 2008; Ridge, 2014)

attempt to have ‘the best of both worlds’ by taking moral sentences to express beliefs *and* non-cognitive attitudes. However, such approaches, in the end, fall prey to the standard problems for cognitivism or expressivism, and fail to properly explain the connection between the two alleged components of moral judgments.

According to inferential expressivism about normative vocabulary, the connection between assent to *Murdering is wrong* and the attitude of disapproval is clearly articulated by the rules of inference for *wrong*. Moreover, we have demonstrated that this approach solves the original version of the Frege-Geach problem as well as the negation version and iterations thereof. In particular, it improves on Schroeder’s (2008a) A-type theory, which assigns the same meaning to *Murdering is wrong* and *Murdering might be wrong*. We submit that inferential expressivism, like traditional expressivism, also has the resources to explain the motivating power of moral judgments, since on this view ‘*murdering is wrong*’ commits the speaker to having the attitude of disapproval towards ‘*murdering*’. If this claim can be made out, inferential expressivism might well be the best of both worlds.¹⁴

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¹⁴This work has received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (grant agreement No 758540) within the project *From the Expression of Disagreement to New Foundations for Expressivist Semantics*.

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